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where $\Gamma_{t} \stackrel{\text { def }}{=}-\ln \left(1-F_{t}\right)=-\ln G_{t}$




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$$
\begin{aligned}
& \qquad \begin{array}{ll}
\mathbb{E}\left(H_{t} \mid \mathcal{G}_{s}\right)=H_{s}+\mathbb{1}_{s<\tau} \frac{1}{G_{s}} \mathbb{E}\left(A_{t}-A_{s} \mid \mathcal{F}_{s}\right) \\
\text { Indeed, } \\
\qquad \begin{aligned}
\mathbb{E}\left(H_{t} \mid \mathcal{G}_{s}\right) & =1-\mathbb{P}\left(t<\tau \mid \mathcal{G}_{s}\right)=1-\mathbb{1}_{s<\tau} \frac{1}{G_{s}} \mathbb{E}\left(G_{t} \mid \mathcal{F}_{s}\right) \\
& =1-\mathbb{1}_{s<\tau} \frac{1}{G_{s}} \mathbb{E}\left(1-Z_{t}-A_{t} \mid \mathcal{F}_{s}\right) \\
& =1-\mathbb{1}_{s<\tau} \frac{1}{G_{s}}\left(1-Z_{s}-A_{s}-\mathbb{E}\left(A_{t}-A_{s} \mid \mathcal{F}_{s}\right)\right) \\
& =1-\mathbb{1}_{s<\tau} \frac{1}{G_{s}}\left(G_{s}-\mathbb{E}\left(A_{t}-A_{s} \mid \mathcal{F}_{s}\right)\right)
\end{aligned}
\end{array} .
\end{aligned}
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(b) Let us prove that (i) implies (ii). Note that $\mathbb{E}\left(\eta_{t} \mid \mathcal{F}_{t}\right)$ is $\mathcal{F}_{t}$ hence
$\mathcal{F}_{\infty}$-measurable. From the definition of conditional expectation (ii) is
equivalent to: for any bounded $\mathcal{F}_{\infty}$-measurable r.v. $\xi$
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$\mathbb{E}_{\mathbb{P}}\left(\xi \mid \mathcal{G}_{t}\right)=\mathbb{E}_{\mathbb{P}}\left(\xi \mid \mathcal{F}_{t}\right)$.

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$$
\begin{aligned}
& \text { Let } \mathbb{Q} \text { be a probability measure equivalent to } \mathbb{P} \text { on }\left(\Omega, \mathcal{G}_{t}\right) \text { for every } t \in \mathbb{R}_{+} \text {, } \\
& \text { with the associated Radon-Nikodým density process } \eta \text {. If the density } \\
& \text { process } \eta \text { is } \mathbb{F} \text {-adapted then we have }
\end{aligned}
$$



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We have thus established the required properties, namely, the probability
law of $\Theta$ and its independence of the $\sigma$-field $\mathcal{F}_{\infty}$. Furthermore,
$\tau=\inf \left\{t: \Gamma_{t}>\Gamma_{\tau}\right\}=\inf \left\{t: \Gamma_{t}>\Theta\right\}$.

## ${ }_{n-} \partial={ }_{n_{\mathcal{J}-}} \partial=\left({ }^{\infty} \mathcal{X} \mid n<\Theta\right) d$

where $C$ is the right inverse of $\Gamma$, so that $\Gamma_{C_{t}}=t$. Therefore
$\cdot\left\{\perp>{ }^{7} D\right\}=\{\perp \mathrm{I}>7\}=\{\Theta>7\}$ Let us set $\Theta \stackrel{\text { def }}{=} \Gamma_{\tau}$. Then
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Here, $\mathbb{F}$ is the filtration of the observations of $V$ at discrete times $t_{1}, \cdots t_{n}$
where $t_{n} \leq t<t_{n+1}$, i.e.,

$$
F_{t}=1-\Phi\left(t-t_{1}, a-X_{t_{1}}\right)\left[1-\exp \left(-\frac{2 a}{t_{1}}\left(a-X_{t_{1}}\right)\right)\right] .
$$

The case $X_{t_{1}} \leq a$ corresponds to default: for $X_{t_{1}} \leq a, F_{t}=1$.

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case, $(\mathrm{H})$ hypothesis is not satisfied.
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[^0]

is continuous at time
$\mathbb{E}\left(U_{T} \mid \mathcal{G}_{t}\right)=\mathbb{E}\left(X \mathbb{1}_{\{T<\tau\}} \mid \mathcal{G}_{t}\right)=U_{t}-\mathbb{E}\left(e^{\Lambda_{\tau}} \Delta Y_{\tau} \mathbb{1}_{\tau<T} \mid \mathcal{G}_{t}\right)$.
and








Let $\phi_{t}^{0}=V_{t}(\phi)-\sum_{i=1}^{2} \phi_{t}^{i} S_{t}^{i}\left(\kappa_{i}\right)$, where the process $V(\phi)$ is given by



[^0]:    Intensity approach
    In the so-called intensity approach, the default tim
    time. The intensity is defined as any non-negative

