



ұӘצ.ЛеIN ӨЧ工
We assume that $F(t)<1, \forall t$













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We introduce the increasing hazard function $\Gamma$ defined by


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- A payment of $\delta(\tau)$ monetary units, where $\delta$ is a deterministic
function, made at time $\tau$ if $\tau<T$.
Here, we do not assume that $F$ is differentiable.
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\begin{aligned}
& \text { әчц } \\
& \text { dynamics }
\end{aligned}
$$








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Proof: We shall give 3 different arguments, each of which constitutes a
proof.
a) Since the function $\gamma$ is deterministic, for $t>s$

b) Another method is to apply integration by parts formula to the
process $L_{t}=\left(1-H_{t}\right) \exp \left(\int_{0}^{t} \gamma(s) d s\right)$ If $U$ and $V$ are two finite
variation processes, Stieltjes' integration by parts formula can be
written as follows
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$\cdot\left((\perp) y^{\perp>7} \mathbb{I}\right) \mathbb{d} \mathbb{H} \mathbb{H}_{(\not))_{\mathrm{I}}} \partial=(\neq) 6$
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where $h$ is a strictly positive fonction, such that $\mathbb{E}_{\mathbb{P}}(h(\tau))=1$. Let
$\Gamma^{*}(t)=-\ln \mathbb{P}^{*}(\tau>t)$. If $\Gamma$ is continuous, $\Gamma^{*}$ is continuous and
$\mathbb{\mathbb { P }} p(\perp) Y={ }_{*} \mathbb{\mathbb { C }} p$

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$F_{\mathbb{Q}}(t)=\mathbb{Q}(\tau \leq t)$.


$$
D(t, T)=B(t, T) \mathbb{E}_{\mathbb{Q}}\left(\left[\mathbb{1}_{T<\tau}+\delta \mathbb{1}_{t<\tau \leq T}\right] \mid t<\tau\right) .
$$

Therefore, we can characterize the cumulative function of $\tau$ under $\mathbb{Q}$
from the market prices of the DZC as follows.
It is usual to interpret the absence of arbitrage opportunities as the
existence of an e.m.m. . If DZCs are traded, their prices are given by
the market, and the equivalent martingale measure $\mathbb{Q}$, chosen by the
market, is such that, on the set $\{t<\tau\}$,


following equality holds

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Let $h$ be a (bounded) Borel function. Then, the martingale
$M_{t}^{h}=\mathbb{E}\left(h(\tau) \mid \mathcal{H}_{t}\right)$ admits the representation
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$M_{t}^{h}=\mathbb{E}\left(h(\tau) \mid \mathcal{H}_{t}\right)$ admits the representation

$$
\begin{aligned}
& \quad \mathbb{E}\left(h(\tau) \mid \mathcal{H}_{t}\right)=\mathbb{E}(h(\tau))+\int_{0}^{t \wedge \tau}(h(s)-\tilde{h}(s)) d M_{s}, \\
& \text { where } M_{t}=H_{t}-\Gamma(t \wedge \tau) \text { and } \tilde{h}(t)=-\frac{P^{\infty} h(u) d G(u)}{G(t)} . \\
& \text { Note that } \tilde{h}(t)=M_{t}^{h} \text { on } t<\tau .
\end{aligned}
$$

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rate $r$ is constant.
We assume that the market has chosen a risk-neutral probability $\mathbb{Q}$ and
that $M$ and $\gamma$ are computed w.r.t. $\mathbb{Q}$. We assume here that the interest

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that $M$ and $\gamma$ are computed w.r.t. $\mathbb{Q}$. We assume here that the interest
rate $r$ is constant.
Price dynamics of a survival claim $(X, 0, \tau)$.
Let $(X, 0, \tau)$ be a survival claim. The price of the payoff $\mathbb{1}_{\{T<\tau\}} X$ that
settles at time $T$ is

$$
\begin{aligned}
& =e^{r t} \mathbb{E}_{\mathbb{Q}}\left(\mathbb{1}_{\{T<\tau\}} e^{-r T} X \mid \mathcal{H}_{t}\right) . \\
& \text { rice process is } \\
& \quad d Y_{t}=r Y_{t} d t-Y_{t-} d M_{t}
\end{aligned}
$$

Price dynamics of a recovery claim $(0, Z, \tau)$.
The recovery $Z$ is paid at the time of default.
The ex-dividend price is
$\quad$ p $(7)$ ) $\left({ }^{7} H\right.$
Price dynamics of a recovery claim $(0, Z, \tau)$.
The recovery $Z$ is paid at the time of default.
The ex-dividend price is

$$
S_{t}=e^{r t} \mathbb{E}_{\mathbb{Q}}\left(\mathbb{1}_{\{T \geq \tau>t\}} e^{-r \tau} Z(\tau) \mid\right.
$$

Hence
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by the formula


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